## Electronic properties and chemical bonding of single-walled MoO<sub>3</sub> nanotubes

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The atomic models of cylindrical zigzag- and armchair-like  $MoO_3$  nanotubes are proposed and their electronic structure and chemical bonding indices are studied using the tight-binding band theory.

Carbon nanotubes discovered<sup>1</sup> in 1991 have attracted much attention because of their unique properties.<sup>2,3</sup> Besides carbon, the size effect on properties has been extensively studied on a nanometre scale for various inorganic species.<sup>4–6</sup> In particular, attention has been focused on the preparation and characterization of quasi-one-dimensional *d*-metal oxides such as TiO<sub>2</sub>, V<sub>2</sub>O<sub>5</sub>, Co<sub>3</sub>O<sub>4</sub>, MnO<sub>2</sub>, WO<sub>3</sub>-based nanotubes and nanowires having potential applications as catalysts, electrodes, intercalation hosts for making new materials *etc*. The first theoretical models of the electronic properties of 3*d*-metal oxide nanotubes (TiO<sub>2</sub> and V<sub>2</sub>O<sub>5</sub>) were proposed.<sup>7,8</sup>

Various nanosized structures of MoO<sub>3</sub> (nanobelts, nanoplatelets, nanorods, fibers<sup>9–12</sup> and hollow nanotubes) were synthesised.<sup>13,14</sup> For example, multi-walled MoO<sub>3</sub> nanotubes were prepared<sup>14</sup> using carbon nanotubes as templates. Since the above tubular composites (MoO<sub>3</sub>/C) have a complicated structure and composition and information on atomic distributions inside the tube walls is lacking, the electronic properties of MO<sub>3</sub> nanotubes have not been studied up to now.

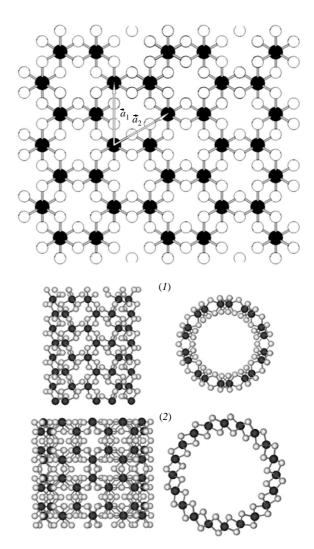
As the first attempt to understand the electronic properties of  $MO_3$  tubes, we performed an atomic simulation of their structure. Here we report the results of quantum-chemical studies of the band structure and chemical bonding as a function of tube diameters (D) and possible geometry types.

Crystalline  $MoO_3$  has  $^{15}$  orthorhombic symmetry (space group Pbnm). It is defined by the lattice constants a=0.392, b=1.394 and c=0.366 nm and comprised of layers, which consist of the infinite chains of corner-sharing  $MoO_6$  units. A view of the structure of a  $MoO_3$  monolayer is shown in Figure 1. The models of molybdenum trioxide infinite-long tubes are constructed by mapping the above two-dimensional  $MoO_3$  monolayer in exactly the same way as for graphene by folding the sheets into seamless cylinders.  $^{2.3}$  Figure 1 illustrates this procedure and the atomic models of some tubes, which represent possible spiral arrangements of  $MoO_6$  chains. Note that  $MoO_3$  nanotubes, as compared with graphene-like tubes, are 'perforated' and contain wall pores inside the rings formed by  $MoO_6$  units.

These 'single-walled' tubes consist of coaxial O–Mo–O cylinders; the tube geometry was determined by the basis vectors  $(a_1 \text{ and } a_2)$  of the Mo atomic sheet introducing the so-called chiral vector  $c_h = na_1 + ma_2$ , whose modulus equals the perimeter of the molybdenum cylinder. In this way, three groups of MoO<sub>3</sub> nanotubes can be obtained depending on the rolling direction  $c_h$ . In terms of carbon-like nanotubes<sup>2,3</sup> they may be defined as non-chiral armchair (n,n)-, zigzag (n,0)-, and chiral (n,m)-like nanotubes.

We calculated the electronic structures of (n,0) and (n,n) MoO<sub>3</sub> nanotubes as a function of n in the ranges (3,0)–(23,0) and (3,3)–(23,23), which correspond to the intervals of the 'central' Mo cylinder diameters  $(D^{\text{Mo}})$  0.470–3.605 and 0.814–6.243 nm, respectively (Table 1). The tight-binding band structure approach within the extended Hückel theory (EHT) approximation<sup>16</sup> was employed. The densities of electronic states (DOS), crystal orbital overlap populations (COOP) and the total band energies of nanotubes  $(E_{\text{tot}})$  were obtained.

The calculated DOSs of all (n,n) and (n,0)-like MoO<sub>3</sub> nanotubes are similar and consistent with the DOS of crystalline molybdenum trioxide. The results indicate that the MoO<sub>3</sub> nanotube valence bands are composed of hybridised O 2p-Mo 4d states; however, the main contributions to the occupied bands



**Figure 1** The structures of molybdenum trioxide monolayer  $(\bar{a}_1$  and  $\bar{a}_2$  are the basis vectors of the Mo sheet) and (1),(2) - armchair (5,5)- and zigzag (10,0) MoO<sub>3</sub> nanotubes. Side views and views along the tube axis are shown.

come from the O 2p states. The lower near-Fermi part of the conduction band is formed predominantly by Mo 4d states. The tube geometry and diameter affect most distinctly the band gap width (BG), see Figure 2. For the nanotubes with a maximum diameter, the BG values are ~4.0 [(23,0)nanotube] and ~3.8 eV [(23,23)nanotube]. While in the EHT the BG is expected to be overestimated, our results are in reasonable agreement with the calculated and observed data for the insulating MoO<sub>3</sub> crystal.  $^{17-19}$  The BG size decreases with decreasing nanotube diameter, whereas the BG values for zigzag-like nanotubes are still higher than those for the armchair-like nanotubes.

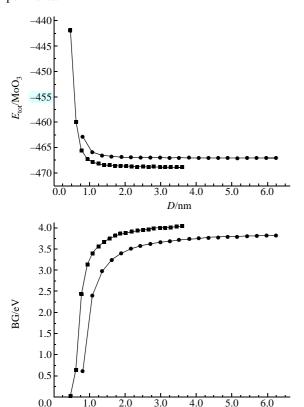
Figure 2 shows the calculated values of  $E_{\text{tot}}$  (per MoO<sub>3</sub> unit) as a function of nanotube diameter. The  $E_{\text{tot}}$  dependence indicates that the stability of MoO<sub>3</sub> tubes diminishes abruptly when D decreases starting from D of about 1 nm. Oppositely, with an

**Table 1** The diameters (D/nm) and indices of intra-atomic bonds (COOPs/e) for MoO $_3$  nanotubes.

Tube	Diameters <sup>a</sup>			$\mathrm{COOPs}^b$			
	D(Oin)	D(Oout)	D(Mo)	Mo-O <sup>in</sup> along	Mo-Oin across	Mo-Oout along	Mo-Oout across
(5,0)	0.471	0.961	0.783	0.200	0.309	0.452	0.370
(10,0)	1.298	1.768	1.567	0.296	0.348	0.417	0.371
(15,0)	2.094	2.562	2.351	0.322	0.356	0.402	0.370
(20,0)	2.884	3.350	3.134	0.333	0.359	0.393	0.370
(5,5)	1.093	1.562	1.357	0.291	0.349	0.472	0.367
(10,10)	2.194	2.659	2.443	0.327	0.370	0.439	0.365
(15,15)	3.829	4.294	4.072	0.340	0.374	0.428	0.364
(20,20)	5.189	5.654	5.429	0.346	0.376	0.422	0.363

 $^aD(\text{Mo})$  and  $D(\text{O}^{\text{in,out}})$  are the diameters of cylinders made of molybdenum and oxygen atoms (Figure 1).  $^b\text{Mo-O}^{\text{in}}$  and Mo-O<sup>out</sup> are the couplings of molybdenum with oxygen atoms of the 'inner' and 'outer' cylinders.

increase in D, the  $E_{\text{tot}}$  is almost constant. This differs noticeably from analogous dependences ( $\sim 1/D^2$ ) of strain energy (the difference between the energies of the plane atomic layer and the corresponding nanotube characterises the chemical stability of tubular structures) known for carbon<sup>2,3</sup> and non-carbon tubes of layered phases (BN,  $\mathrm{MoS}_2$ ,  $\mathit{etc}.^{4-6}$ ). Obviously, the reason has to do with the differences in chemical interactions in MoO<sub>3</sub> and the above quasi-two-dimensional materials. In these materials, the atoms within the layers are bound by strong covalent interactions; bonding between the layers is very weak and is determined by van der Waals forces, and these materials show high propensity to form curve (cylindrical) nanostructures. On the contrary, for d-metal oxides (including MoO<sub>3</sub>), the interatomic bonds are less anisotropic, and intra- and interlayer bonds are comparable. Therefore, d-metal oxide nanotubes can be prepared<sup>6</sup> with the participation of different templates, including carbon nanotubes. 14 This feature is likely to explain the preferably faceted morphology of MoO<sub>3</sub> tubes observed in experiments. 13



**Figure 2** Band gaps and total energies (per  $MoO_3$  unit) as functions of the diameter of molybdenum cylinders for  $MoO_3$  tubes of  $(\bullet)$  armchair and  $(\blacksquare)$  zigzag-like configurations.

D/nm

The covalent bonds coupling scheme in  $MoO_3$  tubes can be seen from the COOP values (Table 1). For all the nanotubes, the main bonds are Mo–O, whereas the Mo–Mo and O–O covalent bonds are practically absent (COOPs ~ 0). There is a considerable anisotropy of the bonds of molybdenum and oxygen atoms (preferentially for the tubes having smaller D) belonging to inner ( $O^{in}$ ) or outer ( $O^{out}$ ) oxygen cylinders, which also depends on the orientation of paired Mo–O bonds along or across the tube axis.

Thus, the atomic models of cylindrical single-walled MoO<sub>3</sub> nanotubes were constructed and their electronic properties and chemical bonding parameters (COOPs) were studied using the tight-binding band theory. We found that zigzag- and armchair-like MoO<sub>3</sub> nanotubes are insulating, and the band gap trends to vanish for small nanotube diameters. The Mo–O covalent bonds were the strongest interactions in the trioxide tubes.

In conclusion, the above models of MoO<sub>3</sub> nanotubes with holey wall structures (large porosity) make it possible to dope these materials with various atoms, which is interesting from the point of view of intercalation processes. The role of MoO<sub>3</sub> nanotube layer numbers (in multi-layered tubes) and the electronic properties of actually produced<sup>14</sup> faceted MoO<sub>3</sub>/carbon nanotubular composites invite further investigation.

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